

Lab. 12 Example solution

# **DESIGN AND CHARACTERIZATION OF SINGLE-END OPA**

# 1. Design of OPA - the phase compensation

$$\omega_u \cong \frac{g_{m1}}{C_C} \quad \omega_{p2} \cong \frac{g_{m6}}{C_L} \quad \omega_z \cong \infty \quad (\text{Zero cancel})$$

The constraint among  $g_{m1}$  and  $g_{m6}$  can be eliminated by the zero-nulling circuit. Thus, say  $g_{m6} = 2g_{m1}$ . In the condition of phase compensation,

$$\omega_{p2} > 2\omega_u$$

$$\frac{g_{m6}}{C_L} > 2 \frac{g_{m1}}{C_C}$$

$$C_C > 2C_L \frac{g_{m1}}{g_{m6}} = C_L = 1.0 \text{pF}$$

The larger capacitance value of  $C_C$  should be chosen to be on the safe side. For example,  $C_C = 4.0 \text{pF}$ .

## 2. Design of OPA - GBP

$$\text{GBP} = \omega_u = \frac{g_{m1}}{C_C}$$

$$g_{m1} = C_C \cdot \text{GBP} = 4.0 \text{pF} \cdot 2\pi \cdot 10 \text{MHz} = 251 \mu\text{S}$$

$$g_{m1} = \sqrt{2\beta_1 I_{DS1}} \quad \beta_1 = \frac{g_{m1}^2}{2I_{DS1}} \quad I_{DS1} = \frac{I_{SS}}{2} = 20 \mu\text{A}$$

$$\begin{aligned} \left(\frac{W}{L}\right)_1 &= \left(\frac{W}{L}\right)_2 = \frac{g_{m1}^2}{2\mu_n C_{OX} I_{DS1}} = \frac{(251 \mu\text{S})^2}{2 \cdot 98 \mu\text{A/V}^2 \cdot 20 \mu\text{A}} = 16.07 \approx 16 \\ &= 32 \mu\text{m}/2 \mu\text{m} = \underbrace{(16 \mu\text{m}/2 \mu\text{m})}_{W/L} * \underbrace{2}_{M} \end{aligned}$$

### 3. Design of OPA - the maximum common-mode voltage

$$V_{in}^{max} = VDD - \Delta_{OV3} - |V_{Tp}| + V_{Tn}$$

$$\Delta_{OV3} = \sqrt{\frac{2I_{DS3}}{\beta_3}} = VDD - |V_{Tp}| + V_{Tn} - V_{in}^{max}$$

$$\beta_3 = \frac{2I_{DS3}}{(VDD - |V_{Tp}| + V_{Tn} - V_{in}^{max})^2}$$

$$\begin{aligned} \left(\frac{W}{L}\right)_3 &= \left(\frac{W}{L}\right)_4 = \frac{2I_{DS3}}{\mu_p C_{OX}} \frac{1}{(VDD - |V_{Tp}| + V_{Tn} - V_{in}^{max})^2} \\ &= \frac{2 \cdot 20\text{uA}}{33\text{uA/V}^2} \frac{1}{(2.5\text{V} - 0.86\text{V} + 0.78\text{V} - 2.2\text{V})^2} = 25.04 \approx 25 = 50\text{u}/2\text{u} = (10\text{u}/2\text{u}) * 5 \end{aligned}$$

# 4. Design of OPA - the minimum common-mode voltage

$$\Delta_{OV1} = \sqrt{\frac{2I_{DS1}}{\beta_1}} = \sqrt{\frac{2 \cdot 20\mu A}{98\mu A/V^2 \cdot 16}} = 0.160V$$

$$V_{in}^{min} = VSS + V_{Tn} + \Delta_{OV1} + \Delta_{OV5}$$

$$\Delta_{OV5} = \sqrt{\frac{2I_{DS5}}{\beta_5}} = V_{in}^{min} - \Delta_{OV1} - V_{Tn} - VSS$$

$$\beta_5 = \frac{2I_{DS5}}{(V_{in}^{min} - \Delta_{OV1} - V_{Tn} - VSS)^2}$$

$$\begin{aligned} \left(\frac{W}{L}\right)_{5a} &= \left(\frac{W}{L}\right)_{5b} = \frac{1}{2} \left(\frac{W}{L}\right)_5 = \frac{2I_{DS5}}{\mu_n C_{OX} (V_{in}^{min} - \Delta_{OV1} - V_{Tn} - VSS)^2} \\ &= \frac{2 \cdot 20\mu A}{98\mu A/V^2} \frac{1}{(-1.4 - 0.160 - 0.78 + 2.5)^2} = 15.94 \approx 16 = 32\mu/2\mu = (16\mu/2\mu)*2 \end{aligned}$$

# 5. Design of OPA - the systematic offset

From the assumption on the phase compensation,

$$g_{m6} = 2g_{m1} = 2 \cdot 251\mu S = 502\mu S$$

$$\Delta_{OV4} = \sqrt{\frac{2I_{DS4}}{\beta_4}} = \sqrt{\frac{2 \cdot 20\mu A}{33\mu A/V^2 \cdot 25}} = 0.220V$$

$$V_{GS4} = V_{GS6} \rightarrow \frac{I_{DS6}}{I_{DS4}} = \frac{\beta_6}{\beta_4} \quad g_{m6} = \sqrt{2\beta_6 I_{DS6}} = \sqrt{2\beta_6 \frac{\beta_6}{\beta_4} I_{DS4}} = \beta_6 \Delta_{OV4}$$

$$\beta_6 = \frac{g_{m6}}{\Delta_{OV4}}$$

$$\left(\frac{W}{L}\right)_6 = \frac{g_{m6}}{\mu_p C_{OX} \Delta_{OV4}} \frac{1}{\frac{502\mu S}{33\mu A/V^2} \frac{1}{0.220V}} = 69.14 \approx 70 = 140/2 = (10/2)*14$$

$$\left(\frac{W}{L}\right)_7 = \frac{1}{2} \left(\frac{W}{L}\right)_5 \frac{\left(\frac{W}{L}\right)_6}{\left(\frac{W}{L}\right)_4} = \frac{1}{2} 32 \frac{70}{25} = 44.8 \approx 45 = 90\mu/2\mu = (10\mu/2\mu)*9$$

# 6. Design of OPA - zero cancelling

$$\left(\frac{W}{L}\right)_{MC1} = \left(\frac{W}{L}\right)_{MC2} = \left(\frac{W}{L}\right)_{MC3} = \left(\frac{W}{L}\right)_6 = 70 = 140\text{u}/2\text{u} = (10\text{u}/2\text{u}) * 14$$

$$\left(\frac{W}{L}\right)_{MC4} = \left(\frac{W}{L}\right)_7 = 45 = 90\text{u}/2\text{u} = (10\text{u}/2\text{u}) * 9$$

The bias current and quiescent power consumption

$$I_{DS6} = \frac{\beta_6}{\beta_4} I_{DS4} = \frac{70}{25} 20\text{uA} = 56\text{uA}$$

$$I_{bias} = I_{ref} + I_{DS5a} + I_{DS5a} + I_{DS\_MC4} + I_{DS7} = 3 * 20\text{uA} + 2 * 56\text{uA} = 172\text{uA}$$

$$P_{bias} = I_{bias} \cdot (VDD - VSS) = 172\text{uA} \cdot 5.0\text{V} = 860\text{uW}$$

# 7. Design of OPA – other properties

The differential gain

$$\begin{aligned} A_d &= \frac{2\sqrt{\beta_1\beta_6}}{(\lambda_2 + \lambda_4)(\lambda_6 + \lambda_7)} \frac{1}{\sqrt{I_{DS1}I_{DS6}}} = \frac{2\sqrt{\mu_n C_{OX} \left(\frac{W}{L}\right)_1 \mu_p C_{OX} \left(\frac{W}{L}\right)_6}}{(\lambda_2 + \lambda_4)(\lambda_6 + \lambda_7)} \frac{1}{\sqrt{I_{DS1}I_{DS6}}} \\ &= \frac{2\sqrt{98\text{uA/V}^2 \cdot 16 \cdot 33\text{uA/V}^2 \cdot 70}}{(0.0186 + 0.0114)^2} \frac{1}{\sqrt{20\text{uA} \cdot 56\text{uA}}} = 126374 = 102\text{dB} \end{aligned}$$

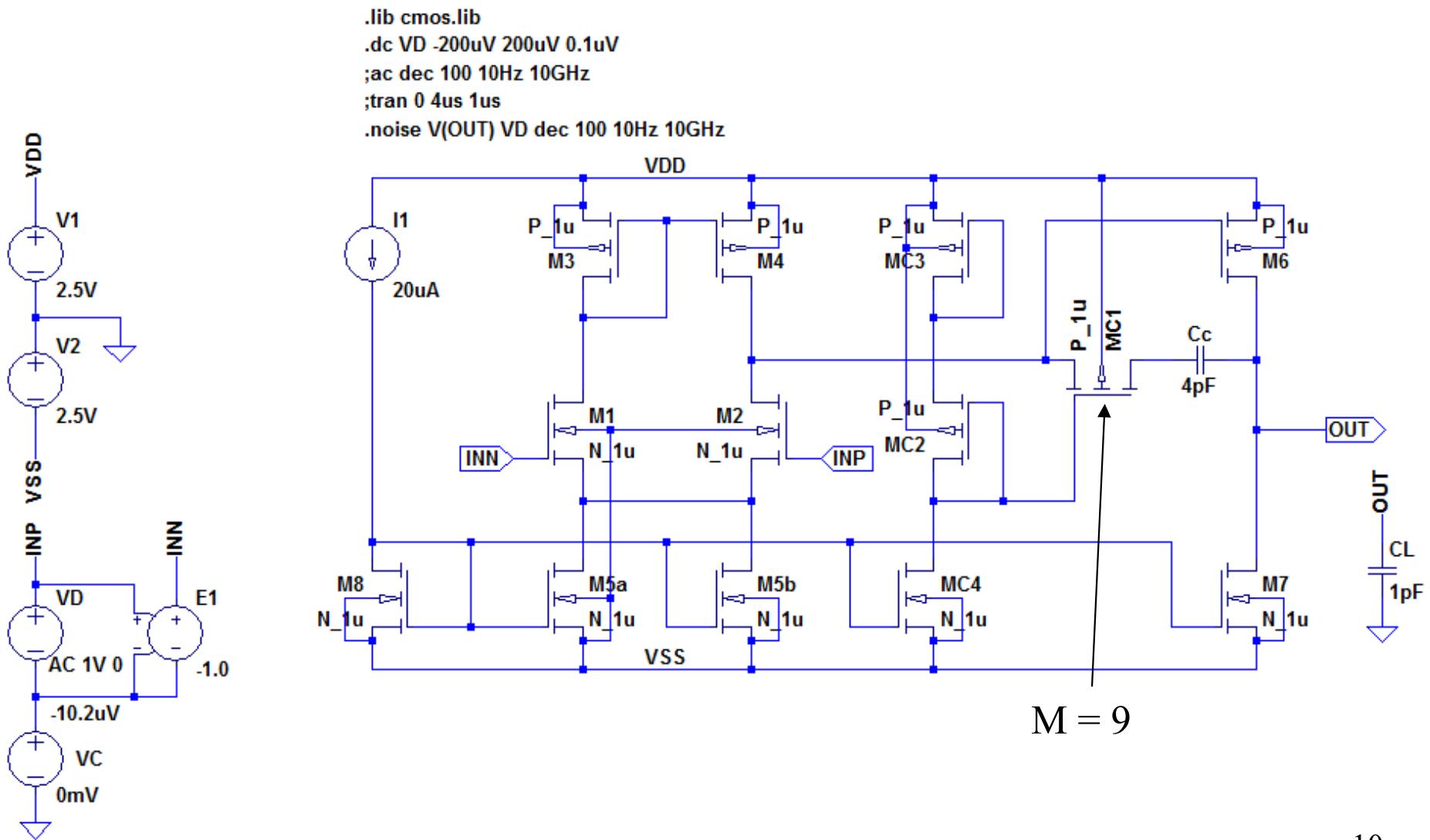
The slew rate

$$SR = \frac{I_{DS5a} + I_{DS5b}}{C_c} = \frac{40\text{uA}}{4.0\text{pF}} = 10\text{V/us}$$

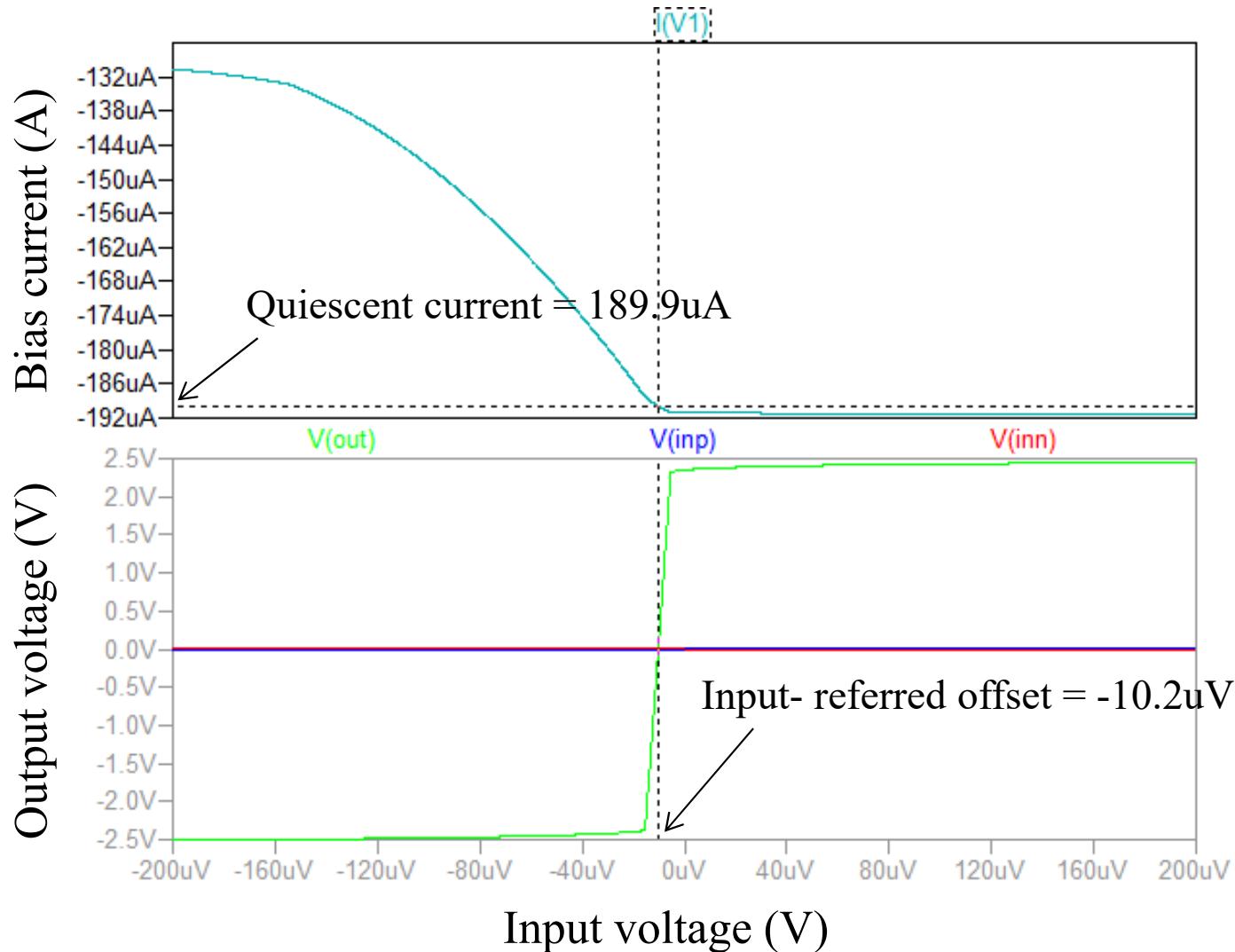
# Schematic

- Draw the schematic of the single-end OPA.
  - or paste the captured schematic with the schematic editor.
- Insert the size ( $L$ ,  $W$ ,  $M$ ) of MOSFET and capacitance value in the schematic.
  - NOTE: The size of MC1 need to be fine-tuned. You have obtained the result  $L = 2\mu$ ,  $W = 10\mu$ ,  $M = 14$ , but use  $L = 2\mu$ ,  $W = 10\mu$ ,  $M = 9$ .

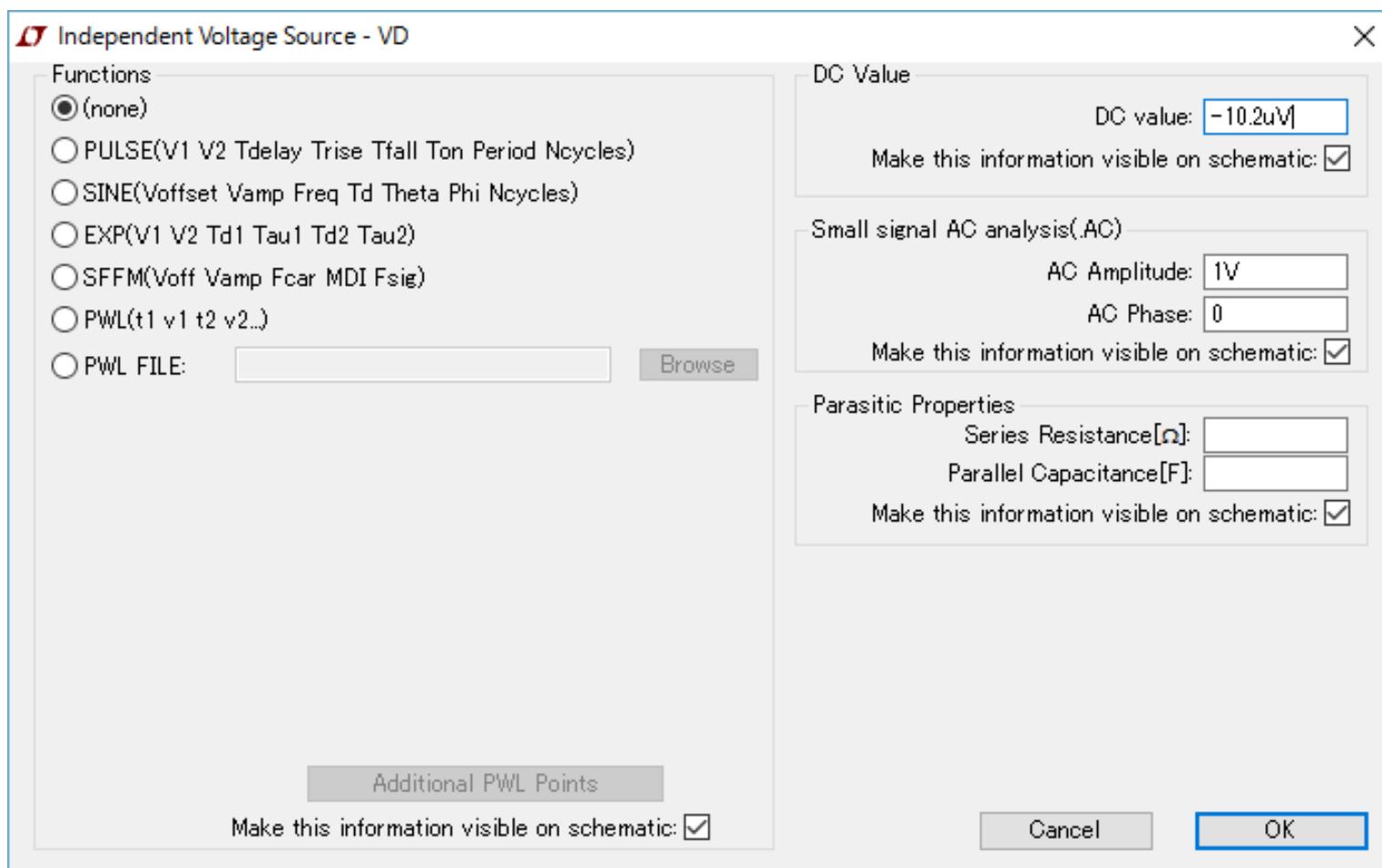
# Characterization of OPA



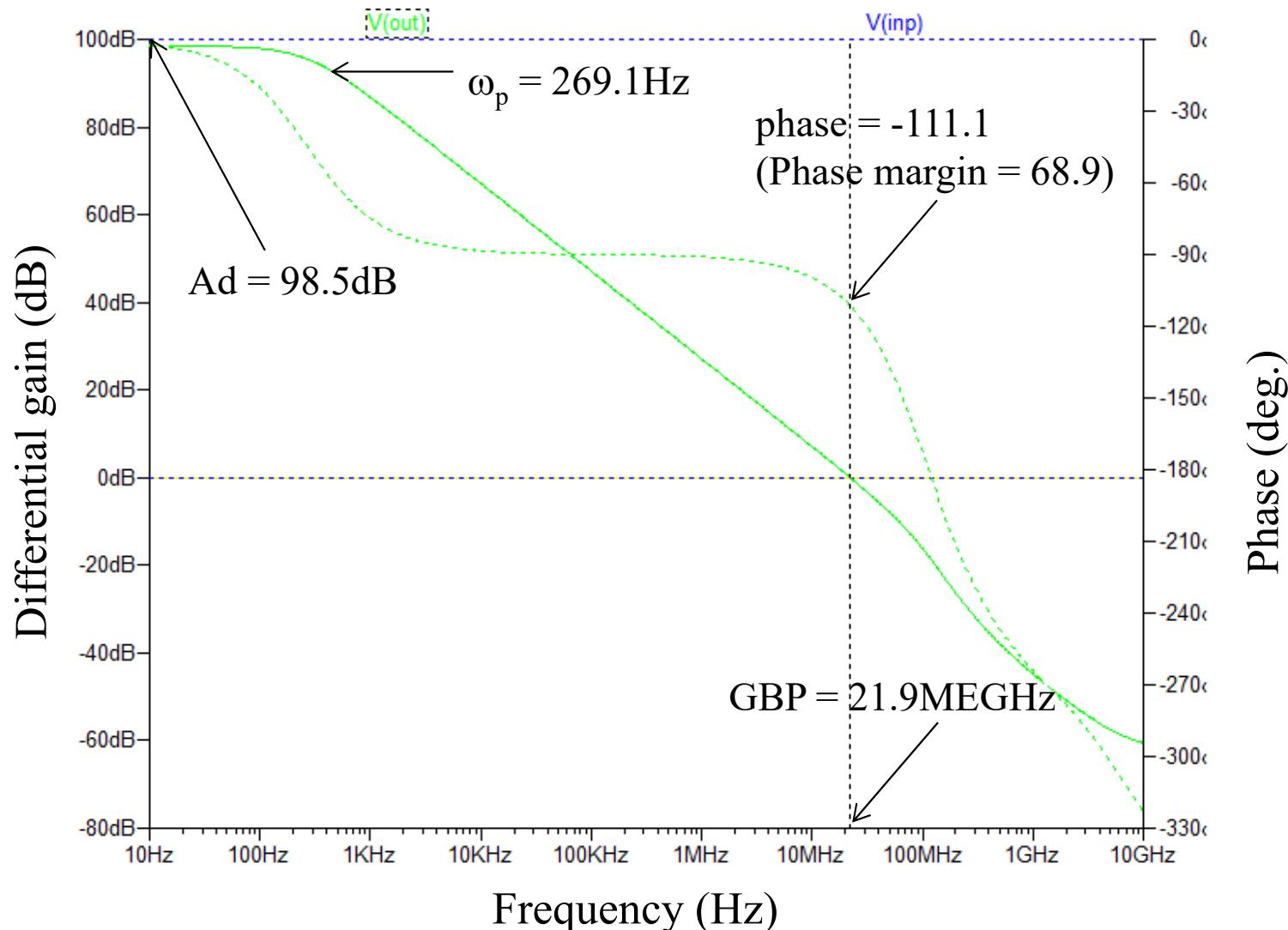
# DC analysis



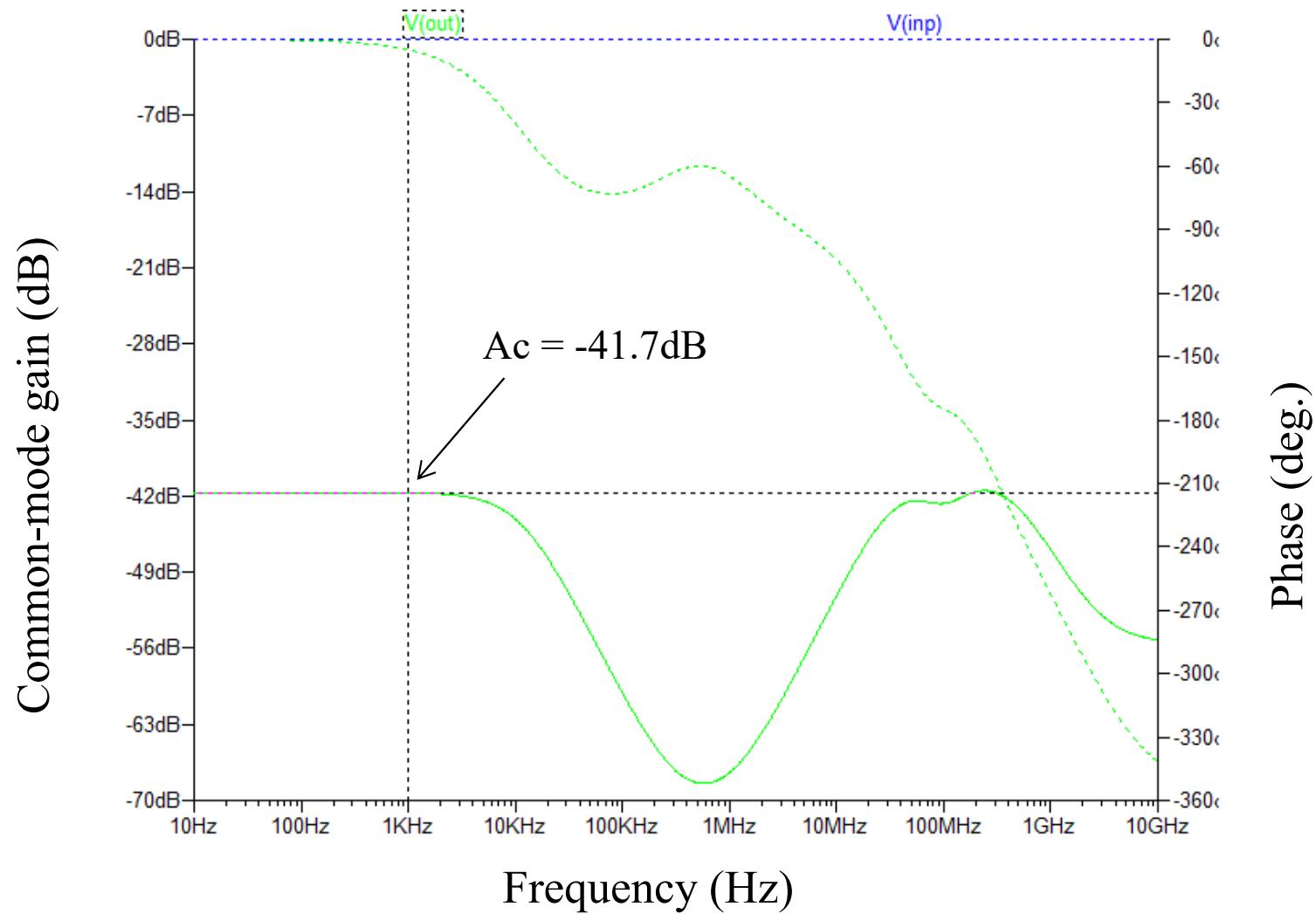
# AC analysis



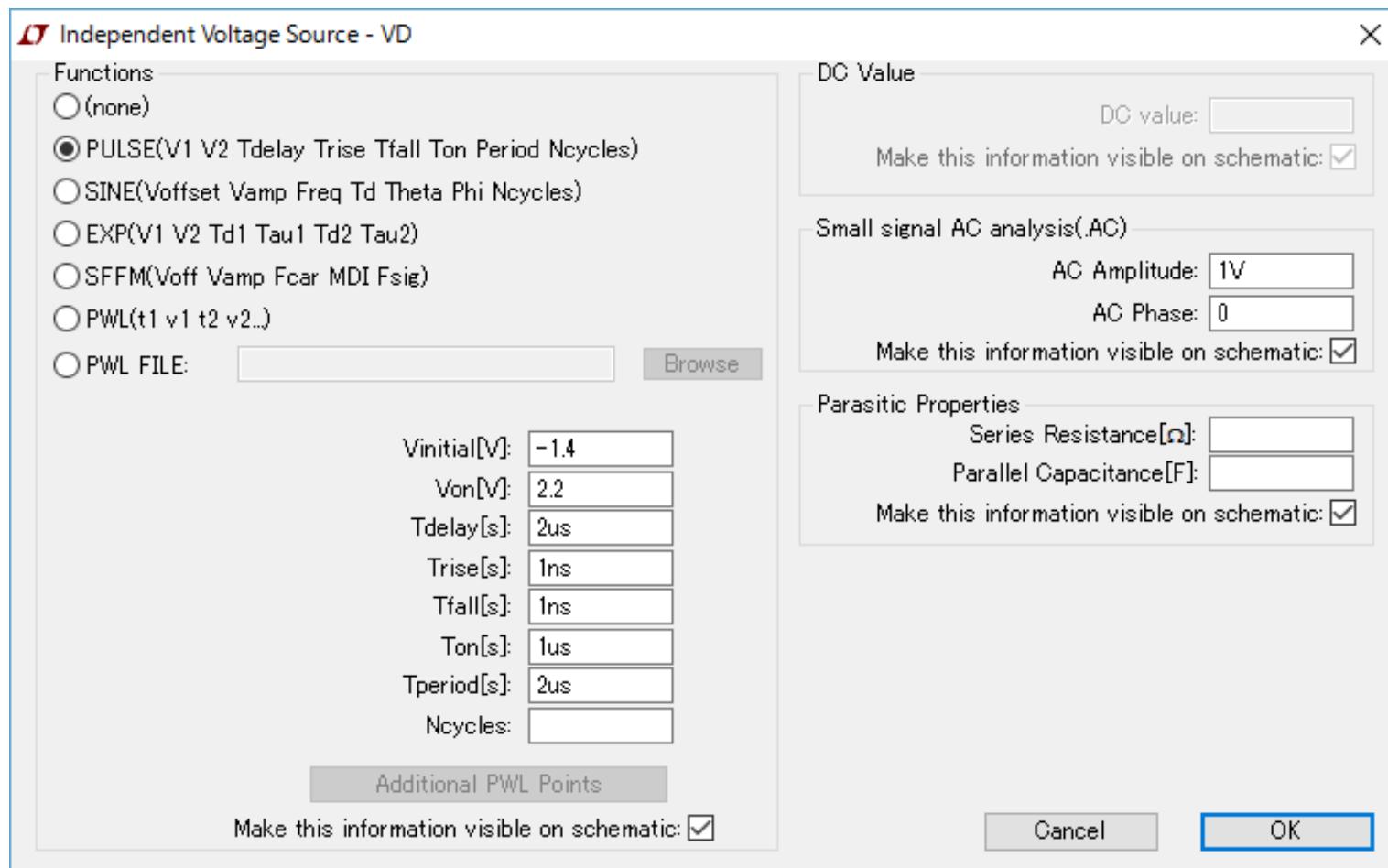
# AC analysis - differential mode



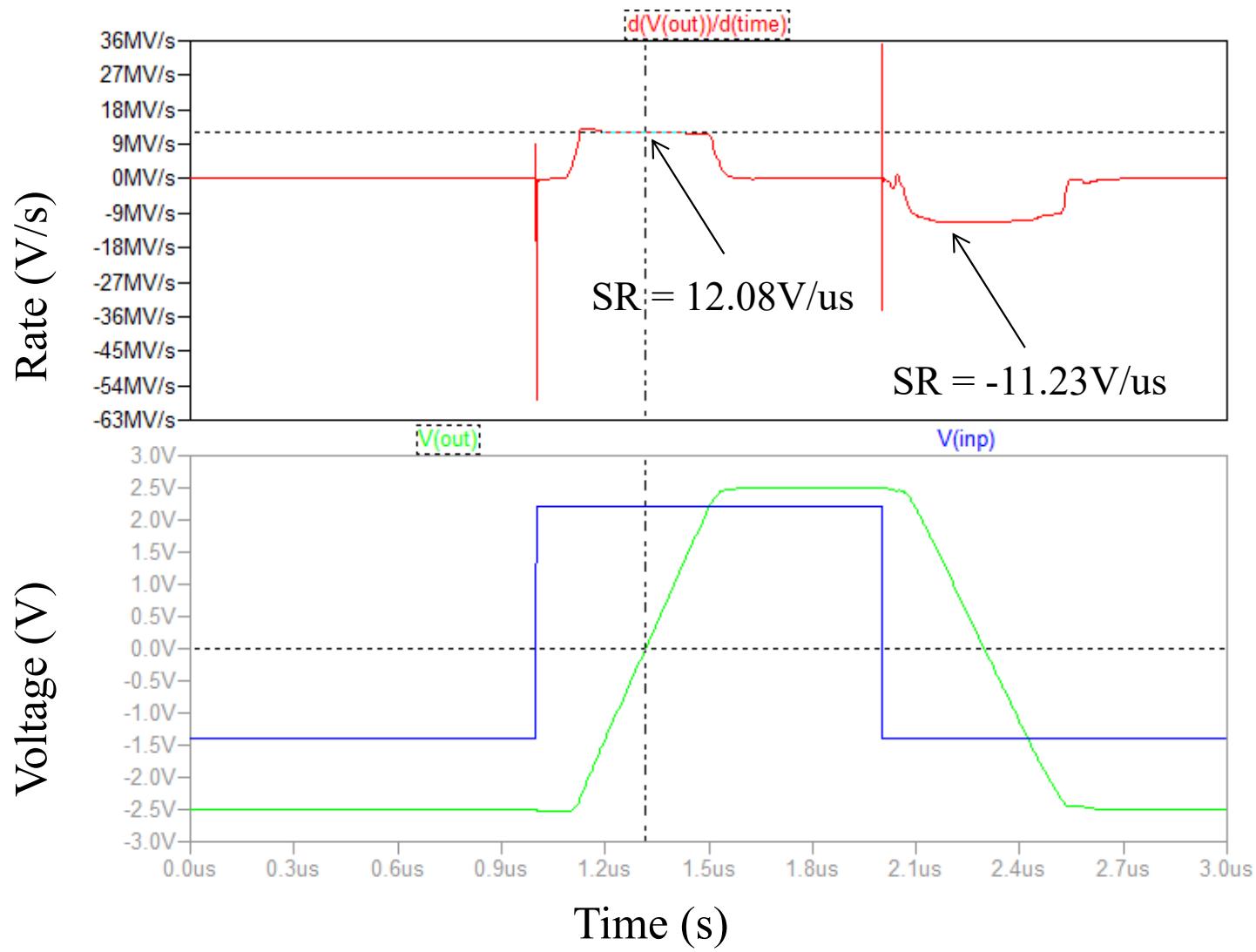
# AC analysis - common mode



# TRAN analysis



# TRAN analysis - step response



# Specification estimated by the circuit simulation

Evaluation item	Unit	Value	Remarks
GBP	MEGHz	21.9	CL = 1.0pF
A <sub>d</sub>	dB	98.5	@ 10Hz
Phase Margin	degree	68.9	
$\omega_p$	Hz	269.1	
A <sub>c</sub>	dB	-41.7dB	@ 1kHz
CMRR	dB	140.2	@ 1kHz
Slew Rate	V/us	11.23	CL = 1.0pF
Offset voltage	uV	-10.2	
Quiescent current	uA	189.9	

# Noise analysis

